

The background of the slide is a photograph of the interior of the CDF II detector. It shows a large, circular structure with various layers of detectors and support structures. The lighting is somewhat dim, with some brighter areas where the detectors are located. The overall color palette is dominated by the metallic and electronic components of the detector.

# Search for $B_{s,d} \rightarrow \mu^+ \mu^-$ Decays at CDF II

**W. Hopkins**

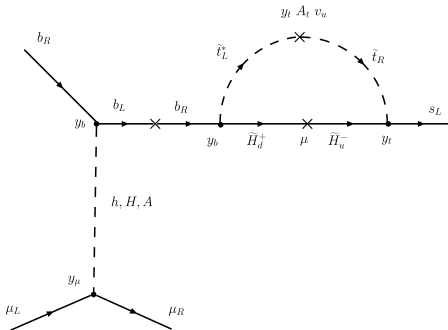
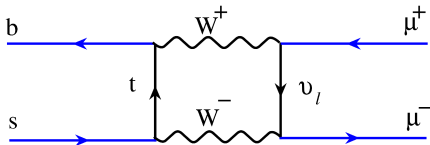
Cornell University

Oct 2011

for the CDF Collaboration

# Motivation

- $B_s \rightarrow \mu^+ \mu^-$  can only occur through higher order FCNC diagrams in Standard Model (SM)
- Suppressed by the GIM Mechanism and helicity
- SM predicts very low rate with little SM background ( $\mathcal{BR}(B_s \rightarrow \mu^+ \mu^-) = (3.2 \pm 0.2) \times 10^{-9}$ ,  $\mathcal{BR}(B_d \rightarrow \mu^+ \mu^-) = (1.0 \pm 0.1) \times 10^{-10}$ , E.Gamiz et al. (HPQCD Collaboration), A.J. Buras et al.
- BSM models predict enhancement
- Ratio of  $\mathcal{BR}(B_s \rightarrow \mu^+ \mu^-)$  and  $\mathcal{BR}(B_d \rightarrow \mu^+ \mu^-)$  is important to discriminate amongst BSM models
- Clean experimental signature



# Analysis Description

## Simple Analysis

- 2 Muons
- Identify methods of suppressing background and keep signal
- Look for bump in di-muon mass distribution

## Analysis Strategy

- Blind ourselves to di-muon signal mass region
- Use mass sidebands to estimate dominant background in signal region
- Optimize selection criteria a priori
- Build confidence in background estimates by employing same methods on control regions

# What do we measure?

$$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) = N_{B_s} \cdot \left[ \frac{1}{N_{B^+}} \frac{\epsilon_{B^+}^{\text{trig}}}{\epsilon_{B_s}^{\text{trig}}} \right] \cdot \left[ \frac{\epsilon_{B^+}^{\text{reco}}}{\epsilon_{B_s}^{\text{reco}}} \frac{\alpha_{B^+}}{\alpha_{B_s}} \frac{1}{\epsilon_{B_s}^{\text{NN}}} \right] \cdot \left[ \frac{f_u}{f_s} \cdot \mathcal{B}(B^+ \rightarrow J/\Psi K^+ \rightarrow \mu^+ \mu^- K^+) \right]$$

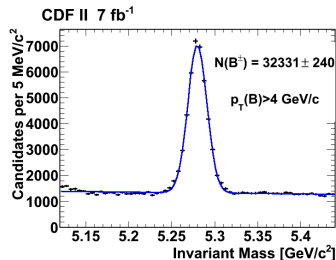
From Data, From MC, From PDG

$$N_{B^+} \sim 2 \times 10^4, \frac{\epsilon_{B^+}^{\text{trig}}}{\epsilon_{B_s}^{\text{trig}}} \sim 1$$

$$\frac{\epsilon_{B^+}^{\text{reco}}}{\epsilon_{B_s}^{\text{reco}}} \sim 1, \frac{\alpha_{B^+}}{\alpha_{B_s}} \sim 0.5, \frac{1}{\epsilon_{B_s}^{\text{NN}}} \sim 1$$

$$\frac{f_u}{f_s} \sim 3, \mathcal{B}(B^+ \rightarrow J/\Psi K^+ \rightarrow \mu^+ \mu^- K^+) \sim 5 \times 10^{-5}$$

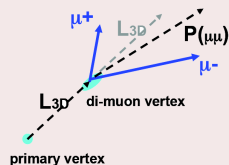
- Measure rate of  $B_s \rightarrow \mu^+ \mu^-$  relative to  $B^+ \rightarrow J/\Psi K^+, J/\Psi \rightarrow \mu^+ \mu^-$
- Apply same selection to find  $B^+ \rightarrow J/\Psi K^+$
- Systematic uncertainties will cancel in ratio, e.g. dimuon trigger efficiency is the same for both modes



# Signal vs. Background

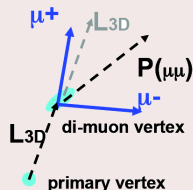
## Signal Properties

- Final state fully reconstructed
- $B_s$  is long lived ( $c\tau \approx 450\mu\text{m}$ )
- $b$  fragmentation is hard: few additional tracks



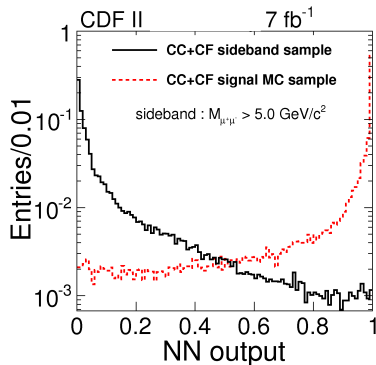
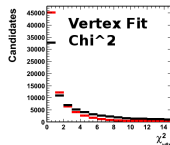
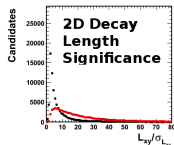
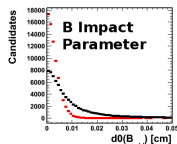
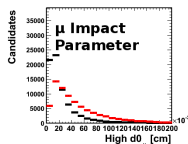
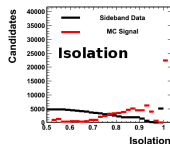
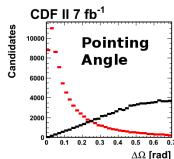
## Background contributions & characteristics

- Sequential semi-leptonic decay:  $b \rightarrow c\mu^- X \rightarrow \mu^+\mu^- X$
- Double semi-leptonic decay:  $bb \rightarrow \mu^-\mu^+ X$
- Continuum  $\mu^-\mu^+$
- $\mu$  + fake and fake+fake
  - Partially reconstructed
  - Softer
  - Short lived
  - Less isolated
- $B \rightarrow hh$ : peaking in signal region



# Signal Discrimination

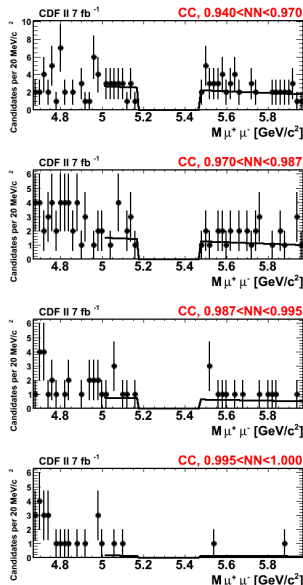
- 14 Discriminating variables
- Invariant mass of muons with  $2.5\sigma$  window,  $\sigma=24$  MeV



- Combined in NN, optimized with signal MC and data mass sideband
- Optimize NN a priori with data mass sideband and signal MC
- Validated NN with normalization mode and control region

# Combinatorial background

- Fit common slope to all sidebands of NN bins
- Exclude region of  $B \rightarrow \mu^+ \mu^- X$  decays from sidebands
- Estimate systematics due to shape uncertainty
- Expect about 0.8 events in most sensitive bin



# Peaking $B \rightarrow hh$ background

- Peaking in signal region
- Estimated using MC and  $D^*$ -tagged  $D^0 \rightarrow \pi^+ K^-$  data
  - MC for  $p_T$  and mass distribution
  - $D^*$ -tagged for fake rate: Ratio of pions/kaons passing muon ID
  - $D^*$ -tagged sample large enough to bin in  $p_T$  and luminosity
- Only 10% of combinatorial background in  $B_s$
- 10x larger in  $B_d$

NN Bin	CC	CF
$0.700 < NN < 0.970$	$0.03 \pm 0.01$	$0.01 \pm < 0.01$
$0.970 < NN < 0.987$	$0.01 \pm < 0.01$	$0.01 \pm < 0.01$
$0.987 < NN < 0.995$	$0.02 \pm < 0.01$	$0.01 \pm < 0.01$
$0.995 < NN < 1.000$	$0.08 \pm 0.02$	$0.03 \pm 0.01$

**Table:**  $B \rightarrow hh$   $B_s$  background for the 3 highest NN bins and the lower 5 bins combined.



# Background Estimate Check

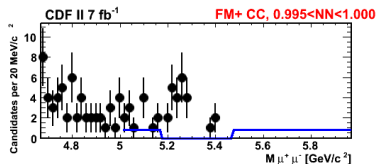
- Check background estimates with background dominated control samples
  - Signal has two opposite sign muons with positive lifetime
  - Control samples have opposite sign negative lifetime, same-sign positive/negative lifetime, and reverse muon ID
  - Total of 64 samples
- Apply same background methods on control sample that we can unblind

NN cut	CC		
	pred	obsv	prob(%)
$0.700 < NN < 0.760$	$217.4 \pm (12.5)$	203	77.7
$0.760 < NN < 0.850$	$262.0 \pm (14.1)$	213	99.1
$0.850 < NN < 0.900$	$117.9 \pm (8.6)$	120	44.7
$0.900 < NN < 0.940$	$112.1 \pm (8.4)$	116	39.4
$0.940 < NN < 0.970$	$112.7 \pm (8.4)$	108	64.2
$0.970 < NN < 0.987$	$80.2 \pm (6.9)$	75	68.3
$0.987 < NN < 0.995$	$67.6 \pm (6.3)$	41	99.8
$0.995 < NN < 1.000$	$32.5 \pm (4.2)$	35	37.5

**Good agreement between observed and expected background**

# $B \rightarrow hh$ Background Check

- Used control sample with reversed muon ID cuts: enhanced in hadrons
  - Total of 16 samples
- Estimated fake rates for this sample using  $D^*$ -tagged for fake rate: Ratio of pions/kaons failing muon ID



## Conclusion

- Checked combinatorial and peaking background estimates with control samples
- Good agreement between predicted and observed

# Expected Sensitivity

$$B_s \rightarrow \mu^+ \mu^- \text{ CC}$$

NN Bin	$\epsilon_{NN}$	B $\rightarrow$ hh Bkg	Total Bkg	Exp SM Signal
$0.700 < NN < 0.970$	20%	0.03	$129.24 \pm 6.50$	$0.26 \pm 0.05$
$0.970 < NN < 0.987$	8%	$< 0.01$	$7.91 \pm 1.27$	$0.11 \pm 0.02$
$0.987 < NN < 0.995$	12%	0.02	$3.95 \pm 0.89$	$0.16 \pm 0.03$
$0.995 < NN < 1.000$	46%	0.08	$0.79 \pm 0.40$	$0.59 \pm 0.11$

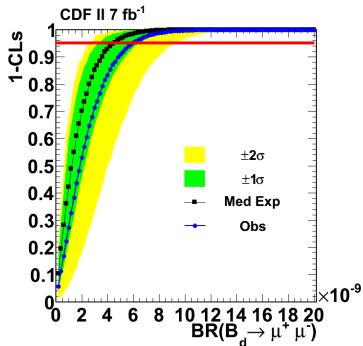
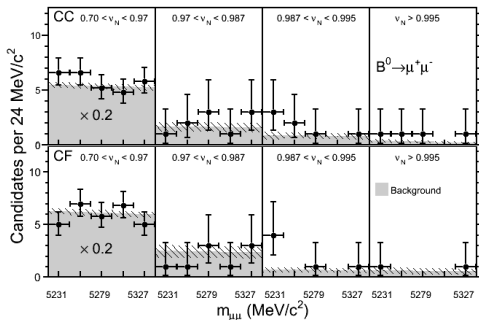
- $\sim 80\%$  signal efficiency for NN
- Small contribution of peaking background compared to combinatorial ( $B_s$ )
- Expect  $\sim 1$  SM signal event

## Expected Limits

$$B_s: 1.5 \times 10^{-8} \text{ at } 95\% \text{ CL}$$

$$B_d: 4.6 \times 10^{-9} \text{ at } 95\% \text{ CL}$$

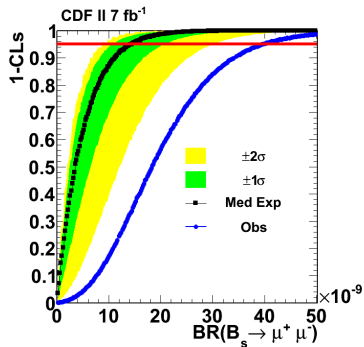
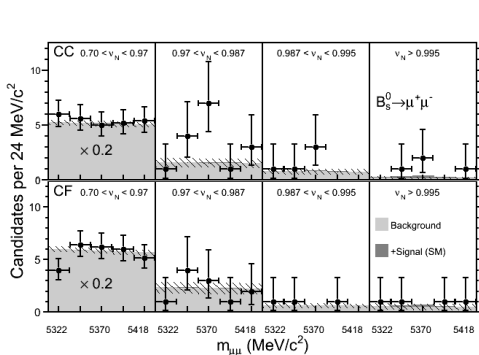
# Results: $B_d$



- Five mass bins
- Five lowest NN bins combined
- Light gray: Background estimates
- Hashed: Systematic errors on background
- Error bars on points: Poisson error on mean
- **No excess in  $B_d$  mass region (p-value=23%)**

**$B_d$  limit:  $\mathcal{B}(B_d \rightarrow \mu^+ \mu^-) < 6.0 \times 10^{-9}$  @ 95% C.L.**

# Results: $B_s$

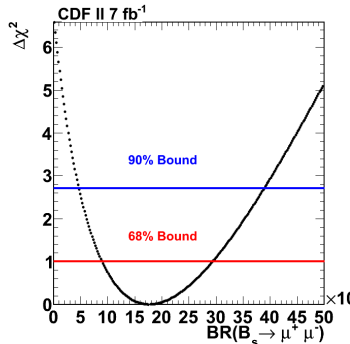


- Dark gray: Expected SM signal
- **Excess in CC**
  - p-value for background only hypothesis: 0.27%
  - p-value for SM+background hypothesis: 1.92%

**$B_s$  limit:**  $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) < 4.0 \times 10^{-8}$  @ 95% C.L. ( $> 2\sigma$  from expected)

# $B_s$ : Central Values, Bounds and P-Values

- Used  $\Delta\chi^2$  method
- Cross checked with Bayesian Posterior method
- Includes all systematics
- 90% Bound:  
 $4.6 \times 10^{-9} < \mathcal{B}(B_s \rightarrow \mu^+ \mu^-) < 3.9 \times 10^{-8}$
- Stable: No large deviation when only using subset of bins



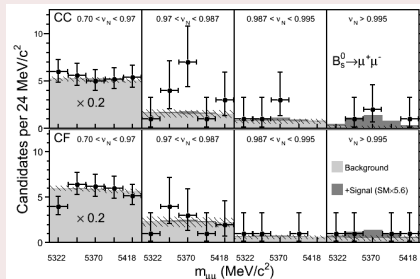
## Summary of p-values and limits

	All Bins	2 Highest NN Bins
Central Value ( $\times 10^{-8}$ )	$1.8^{+1.1}_{-0.9}$	$1.4^{+1.0}_{-0.8}$
90% Bounds ( $\times 10^{-8}$ )	$0.46 < \mathcal{B} < 3.9$	$0.33 < \mathcal{B} < 3.3$
Bkg Only p-value	0.27%	0.66%
SM+Bkg p-value	1.92%	4.14%

# Third NN Bin Excess

## Background Estimate Problem

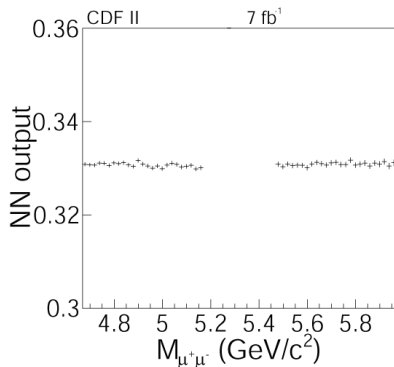
- Combinatorial Background Problem
  - $B_d$  Uses same sideband as  $B_s \Rightarrow$  No excess in  $B_d$
- Peaking Background Problem
  - Only peaking background is  $B \rightarrow hh$
  - 10x larger in  $B_d$  region
  - No excess in  $B_d \Rightarrow$  good fake rates



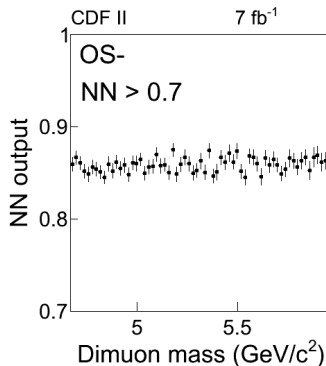
## Neural Network Problem

- Mass bias?
- Overtrained?
- Mismodels data?

## NN Output vs Dimuon Mass for Signal Sample (blinded)



## NN Output vs Dimuon Mass for Control Sample

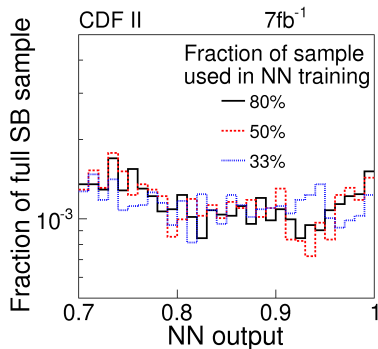


**Unlikely to be cause of excess in 3rd NN bin of CC**

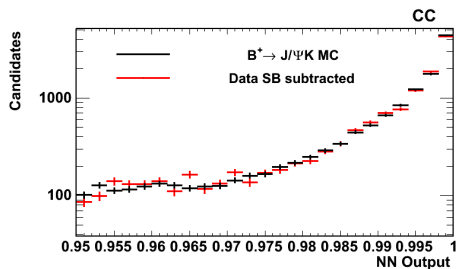


# NN Studies: Overtraining and Mismodeling

**NN SB background eff for NN's trained on different fractions of SB**



**$B^+ \rightarrow J/\psi K^+$  MC and Data Signal NN Output Distribution**



**Unlikely to be cause of excess in 3rd NN bin of CC  
MC models data well**

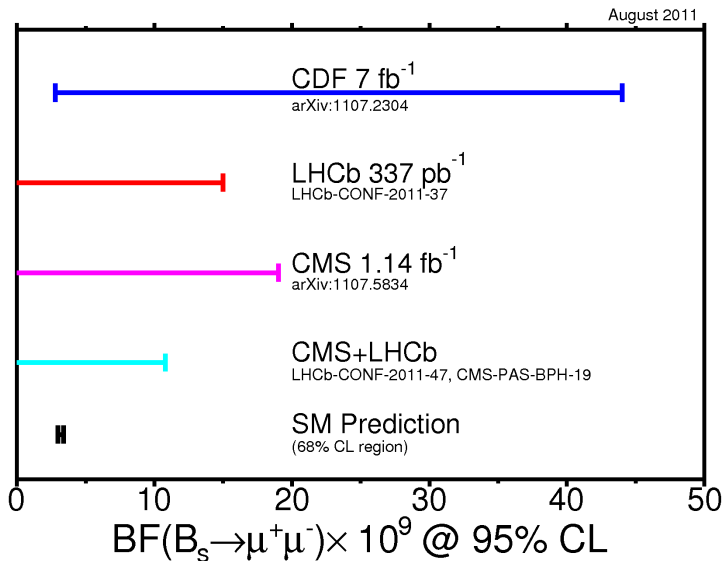
## Conclusion on 3rd NN bin

- Not due to any NN mismodeling
- Not due to background mismodeling
- **Only explanation left: Not unlikely statistical fluctuation in 80 bins**

### From PRL:

In short, there is no evidence that the excess in this bin is caused by a mistake or systematic error in our background estimates or our modeling of the  $\nu_{NN}$  performance and distribution. The most plausible remaining explanation is that this is a statistical fluctuation.

# Current Experimental Status



# Conclusion

- CDF updated the  $B_s \rightarrow \mu^+ \mu^-$  search with doubled dataset ( $7\text{fb}^{-1}$ ) and improved analysis technique
- CDF has excess of  $B_s \rightarrow \mu^+ \mu^-$  events at the level of  $2.7\sigma$  relative to background only hypothesis
- Set the first two-sided bound on the rate:  
 $4.6 \times 10^{-9} < \mathcal{B}(B_s \rightarrow \mu^+ \mu^-) < 3.9 \times 10^{-8}$  at the 90% CL, compatible with SM and other experiments
- Update analysis with full CDF dataset is ongoing

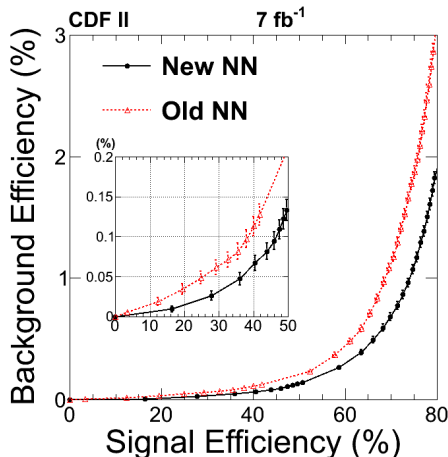
## Backup Slides

# Signal Discrimination

- Optimize NN a priori using data mass sideband and signal MC
- Validated NN with normalization mode and control region
  - Checked for Overtraining
  - Checked for Mass bias
  - Checked MC modeling of data
- Divide data sample into several bins
  - Two muon topologies: Central-Central (CC) and Central-Forward (CF)
  - 8 NN bins ranging between  $0.7 < NN < 1.0$
  - 5 mass bins: Allows mass shape determination

# Analysis Improvements

- $\sim 50\%$  more data
- 20% Increase in acceptance by including CMX miniskirts and COT spacer regions
- Using new  $dE/dx$  calibration for better  $\mu$  ID
- Improved fake rates for peaking background estimates
- New neural network with 2x better background rejection



# Combinatorial Background

NN Bin	CC	CF
$0.700 < NN < 0.970$	$129.2 \pm 6.5$	$146.3 \pm 7.0$
$0.970 < NN < 0.987$	$7.9 \pm 1.9$	$11.6 \pm 1.8$
$0.987 < NN < 0.995$	$4.0 \pm 1.1$	$3.3 \pm 1.0$
$0.995 < NN < 1.000$	$0.79 \pm 0.52$	$2.6 \pm 1.5$

**Table:** Combinatorial  $B_s$  background for the 3 highest NN bins and the lower 5 bins combined.

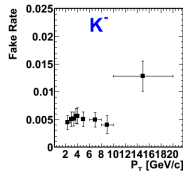
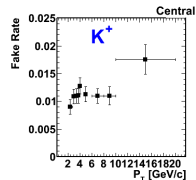
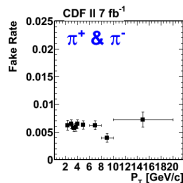
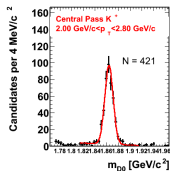
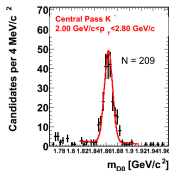
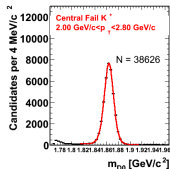
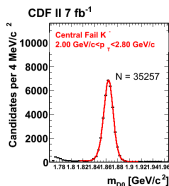
NN Bin	CC	CF
$0.700 < NN < 0.970$	$134.0 \pm 6.6$	$153.4 \pm 7.3$
$0.970 < NN < 0.987$	$8.2 \pm 2.0$	$12.1 \pm 1.9$
$0.987 < NN < 0.995$	$4.1 \pm 1.2$	$3.4 \pm 1.1$
$0.995 < NN < 1.000$	$0.8 \pm 0.5$	$2.8 \pm 1.6$

**Table:** Combinatorial  $B_d$  background.



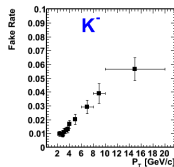
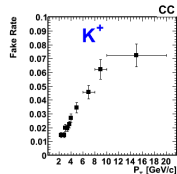
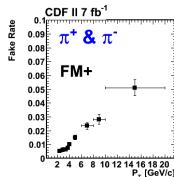
# Fake rates

- Binned in  $p_T$  and instantaneous luminosity



# Fake rates: Pion and Kaon Enhanced Control Sample

- Same procedure as with signal sample but now reversing muon ID cuts (dE/dx and muon likelihood function)



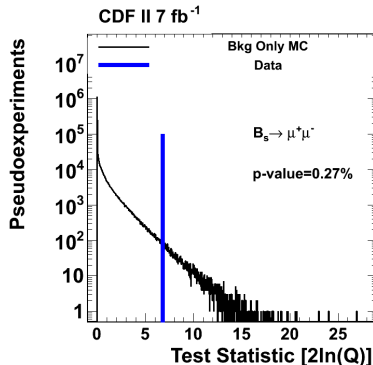
# Expected Sensitivity

	CC		CF	
$(\alpha_{B^+}/\alpha_{B_s})$	$0.307 \pm 0.018$	( $\pm 6\%$ )	$0.197 \pm 0.014$	( $\pm 7\%$ )
$(\epsilon_{B^+}^{trig}/\epsilon_{B_s}^{trig})$	$0.99935 \pm 0.00012$	( $< 1\%$ )	$0.97974 \pm 0.00016$	( $< 1\%$ )
$(\epsilon_{B^+}^{reco}/\epsilon_{B_s}^{reco})$	$0.85 \pm 0.06$	( $\pm 8\%$ )	$0.84 \pm 0.06$	( $\pm 9\%$ )
$\epsilon_{B_s}^{NN}(NN > 0.70)$	$0.915 \pm 0.042$	( $\pm 4\%$ )	$0.864 \pm 0.040$	( $\pm 4\%$ )
$\epsilon_{B_s}^{NN}(NN > 0.995)$	$0.461 \pm 0.021$	( $\pm 5\%$ )	$0.468 \pm 0.022$	( $\pm 5\%$ )
$N_{B^+}$	$22388 \pm 196$	( $\pm 1\%$ )	$9943 \pm 138$	( $\pm 1\%$ )
$f_u/f_s$	$3.59 \pm 0.37$	( $\pm 13\%$ )	$3.59 \pm 0.37$	( $\pm 13\%$ )
$B(B^+ \rightarrow \mu^+ \mu^- K^+)$	$(6.01 \pm 0.21) \times 10^{-5}$	( $\pm 4\%$ )	$(6.01 \pm 0.21) \times 10^{-5}$	( $\pm 4\%$ )
SES (All bins)	$(2.9 \pm 0.5) \times 10^{-9}$	( $\pm 18\%$ )	$(4.0 \pm 0.7) \times 10^{-9}$	( $\pm 18\%$ )

**Combined Single Event Sensitivity (CC+CF) =  $1.7 \times 10^{-9}$**   
**Single Event Sensitivity is now to level of SM**

- Estimated p-values for background only and SM+background hypothesis
- Compare observed with the distribution expected from ensembles of pseudo-experiments
  - background-only
  - background + signal at SM level
- All systematics included in pseudo-experiments

## Background only



$B_s$  background only p-value = 0.27%

$B_s$  SM+background p-value = 1.92%

$B_d$  background only p-value = 23%